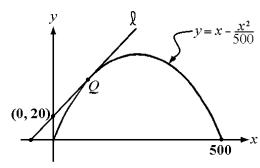
## AP PROBLEM SET 1 DERIVATIVES

(79-1)

- 1. Given the function f defined by  $f(x) = 2x^3 3x^2 12x + 20$ .
- (a) Find the zeros of f.
- (b) Write an equation of the line normal to the graph of f at x = 0.
- (c) Find the x and y coordinates of all points on the graph of f where the line tangent to the graph is parallel to the x-axis.

(96-6)

2.



Line  $\ell$  is tangent to the graph of  $y = x - \frac{x^2}{500}$  at the point Q, as shown in the figure above.

- (a) Find the x-coordinate of point Q
- (b) Write an equation for line  $\ell$ .
- (c) Suppose the graph of  $y = x \frac{x^2}{500}$  shown in the figure, where x and y are measured in feet, represents a hill. There is a 50-foot tree growing vertically at the top of the hill. Does a spotlight at point P directed along line  $\ell$  shine on any part of the tree? Show the work that leads to your conclusion.

(75-5)

- 3. The line x = c where c > 0 intersects the cubic  $y = 2x^3 + 3x^2 9$  at point P and the parabola  $y = 4x^2 + 4x + 5$  at point Q.
- (a) If a line tangent to the cubic at point P is parallel to the line tangent to the parabola at point Q, find the value of c where c > 0.
- (b) Write the equations of the two tangent lines described in (a).

- 4. Let f be the function that is given by  $f(x) = \frac{ax+b}{x^2-c}$  and that has the following properties.
  - (i) The graph of f is symmetric with respect to the y-axis.
  - (ii)  $\lim_{x \to 2^+} f(x) = +\infty$
  - (iii) f'(1) = -2
- (a) Determine the values of a, b, and c.
- (b) Write an equation for each vertical and each horizontal asymptote of the graph of f.
- (c) Sketch the graph of f in the xy-plane.

(86-4)

5. Let f be the function defined as follows.

$$f(x) = \begin{cases} |x-1|+2, & \text{for } x < 1\\ ax^2 + bx, & \text{for } x \ge 1, \text{ where } a \text{ and } b \text{ are constants} \end{cases}$$

- (a) If a = 2 and b = 3, is f continuous for all x? Justify your answer.
- (b) Describe all values of a and b for which f is a continuous function.
- (c) For what values of a and b is f both continuous and differentiable?

(85-1)

- 6. Let f be the function given by  $f(x) = \frac{2x-5}{x^2-4}$
- (a) Find the domain of f.
- (b) Write an equation for each vertical and each horizontal asymptote for the graph of f.
- (c) Find f'(x).
- (d) Write an equation for the line tangent to the graph of f at the point (0, f(0)).