(94-3)

- 1. Consider the curve defined by $x^2 + xy + y^2 = 27$.
- (a) Write an expression for the slope of the curve at any point (x,y).
- (b) Determine whether the lines tangent to the curve at the *x*-intercepts of the curve are parallel. Show the analysis that leads to your conclusion.
- (c) Find the points on the curve where the lines tangent to the curve are vertical.

(73-3)

- 5. Given the curve $x + xy + 2y^2 = 6$.
- (a) Find $\frac{dy}{dx}$.
- (b) Write an equation for the line tangent to the curve at the point (2, 1).
- (c) Find the coordinates of all other points on this curve with slope equal to the slope at (2, 1).

(92-4)

3. Consider the curve defined by the equation $y + \cos y = x + 1$ for $0 \le y \le 2\pi$.

(a) Find
$$\frac{dy}{dx}$$
 in terms of y.

(b) Write an equation for each vertical tangent to the curve.

(c) Find
$$\frac{d^2y}{dx^2}$$
 in terms of y.

(2000-5)

4. Consider the curve given by $xy^2 - x^3y = 6$.

(a) Show that
$$\frac{dy}{dx} = \frac{3x^2y - y^2}{2xy - x^3}$$

- (b) Find all points on the curve whose *x*-coordinate is 1, and write an equation for the tangent line at each of these points.
- (c) Find the *x*-coordinate of each point on the curve where the tangent line is vertical.

(95-3)

5. Consider the curve defined by $-8x^2 + 5xy + y^3 = -149$.

(a) Find $\frac{dy}{dx}$.

- (b) Write an equation for the line tangent to the curve at the point (4, -1).
- (c) There is a number k so that the point (4.2, k) is on the curve. Using the tangent line found in part (b), approximate the value of k.
- (d) Write an equation that can be solved to find the actual value of k so that the point (4.2, k) is on the curve.
- (e) Solve the equation found in part (d) for the value of k.

(2015-6)

- 6. Consider the curve given by the equation $y^3 xy = 2$. It can be shown that $\frac{dy}{dx} = \frac{y}{3y^2 x}$.
- (a) Write an equation for the line tangent to the curve at the point (-1, 1).
- (b) Find the coordinates of all points on the curve at which the line tangent to the curve at that point is vertical.
- (c) Evaluate $\frac{d^2y}{dx^2}$ at the point on the curve where x = -1 and y = 1.