

Homework – Chapter 9 Part I

1. Write the following as a set of values and an interval.

$$\text{a) } x > -5 \quad \{x \in \mathbb{R}, x > -5\} \quad (-5, +\infty)$$

$$\text{b) } x \leq -10 \quad \{x \in \mathbb{R}, x \leq -10\} \quad (-\infty, -10]$$

$$\text{c) } -2 \leq x < 3 \quad \{x \in \mathbb{R}, -2 \leq x < 3\} \quad [-2, 3)$$

$$\text{d) } x < -1 \text{ or } x \geq 4 \quad \{x \in \mathbb{R}, x < -1 \text{ or } x \geq 4\} \quad (-\infty, -1) \cup [4, +\infty)$$

2. Solve:

$$\text{a) } 2(x + 5) - 4 \geq 5(3x - 2)$$

$$2x + 10 - 4 \geq 15x - 10$$

$$-13x \geq -16$$

$$x \leq \frac{16}{13}$$

$$(-\infty, \frac{16}{13}]$$

$$\text{b) } \frac{2}{3}(9x - 12) < 1 - 3(2x - 5)$$

$$6x - 8 < 1 - 6x + 15$$

$$12x < 24$$

$$x < 2$$

$$(-\infty, 2)$$

$$\text{c) } \frac{x+3}{4} \leq -\frac{2x-3}{5}$$

$$5(x+3) \leq -4(2x-3) \quad \downarrow \times 4 \times 5$$

$$5x + 15 \leq -8x + 12$$

$$13x \leq -3$$

$$x \leq -\frac{3}{13}$$

$$(-\infty, -\frac{3}{13}]$$

$$\text{d) } (2x + 1)(3x - 5) \leq 6(x + 1)(x - 1)$$

$$6x^2 - 10x + 3x - 5 \leq 6(x^2 - 1)$$

$$6x^2 - 7x - 5 \leq 6x^2 - 6$$

$$-7x \leq -1$$

$$x \geq \frac{1}{7}$$

$$[\frac{1}{7}, +\infty)$$

$$e) 4(x+3)(x-1) > (2x-3)^2$$

$$4(x^2 - x + 3x - 3) > 4x^2 - 12x + 9$$

$$4x^2 + 8x - 12 > 4x^2 - 12x + 9$$

$$20x > 21$$

$$x > \frac{21}{20}$$

$$\left(\frac{21}{20}, +\infty\right)$$

3. Are the following numbers part of the solution?

a) $x = 5$ for $3x - 5 \leq 2x + 1$

$$\begin{array}{r|l} 3(5) - 5 & 2(5) + 1 \\ 15 - 5 & 10 + 1 \\ 10 & 11 \end{array} \quad \text{yes!}$$

b) $x = -\frac{1}{3}$ for $2(x - 4) > 3x + 2$

$$\begin{array}{r|l} 2\left(-\frac{1}{3} - 4\right) & 3\left(-\frac{1}{3}\right) + 2 \\ 2\left(-\frac{13}{3}\right) & -1 + 2 \\ -\frac{26}{3} & 1 \end{array} \quad \text{no!}$$

c) $x = -3$ for $x^2 - 5x + 2 \geq 0$

$$\begin{array}{r|l} (-3)^2 - 5(-3) + 2 & 0 \\ 9 + 15 + 2 & \\ 26 & \end{array} \quad \text{yes!}$$

d) $x = -\frac{2}{3}$ for $3x^2 - 4x + 5 \leq 0$

$$\begin{array}{r|l} 3\left(-\frac{2}{3}\right)^2 - 4\left(-\frac{2}{3}\right) + 5 & 0 \\ 3\left(\frac{4}{9}\right) + \frac{8}{3} + 5 & \\ \frac{4}{3} + \frac{8}{3} + \frac{15}{3} & \\ \frac{27}{3} & \\ 9 & \end{array} \quad \text{no!}$$